Principles for Predicting RNA Secondary Structure Design Difficulty

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Abstract

Designing RNAs that form specific secondary structures is enabling better understanding and control of living systems through RNA-guided silencing, genome editing and protein organization. Little is known, however, about which RNA secondary structures might be tractable for downstream sequence design, increasing the time and expense of design efforts due to inefficient secondary structure choices. Here, we present insights into specific structural features that increase the difficulty of finding sequences that fold into a target RNA secondary structure, summarizing the design efforts of tens of thousands of human participants and three automated algorithms (RNAInverse, INFO-RNA and RNA-SSD) in the Eterna massive open laboratory. Subsequent tests through three independent RNA design algorithms (NUPACK, DSS-Opt and MODENA) confirmed the hypothesized importance of several features in determining design difficulty, including sequence length, mean stem length, symmetry and specific difficult-to-design motifs such as zigzags. Based on these results, we have compiled an Eterna100 benchmark of 100 secondary structure design challenges that span a large range in design difficulty to help test future efforts. Our *in silico* results suggest new routes for improving computational RNA design methods and for extending these insights to assess "designability" of single RNA structures, as well as of switches for *in vitro* and *in vivo* applications.

Introduction

RNA molecules play important roles in a variety of biological processes such as gene regulation, protein synthesis and viral infection. The folding of RNAs into specific secondary structures is necessary for performing these functions, and numerous methods have been developed to model this folding process [1,2]. Many emerging applications of RNA, including gene silencing, genome editing and creation of complex nanostructures, rely on inverse folding, the design of RNAs that fold into specified secondary structures in their minimum free-energy states [3–5]. Solving the inverse folding problem is an important step in moving toward the design of RNA molecules that carry out desired functions.

Several algorithms have been developed to computationally address the inverse folding problem. The pioneering tool RNAInverse used an adaptive walk, randomly sampling mutations and accepting those
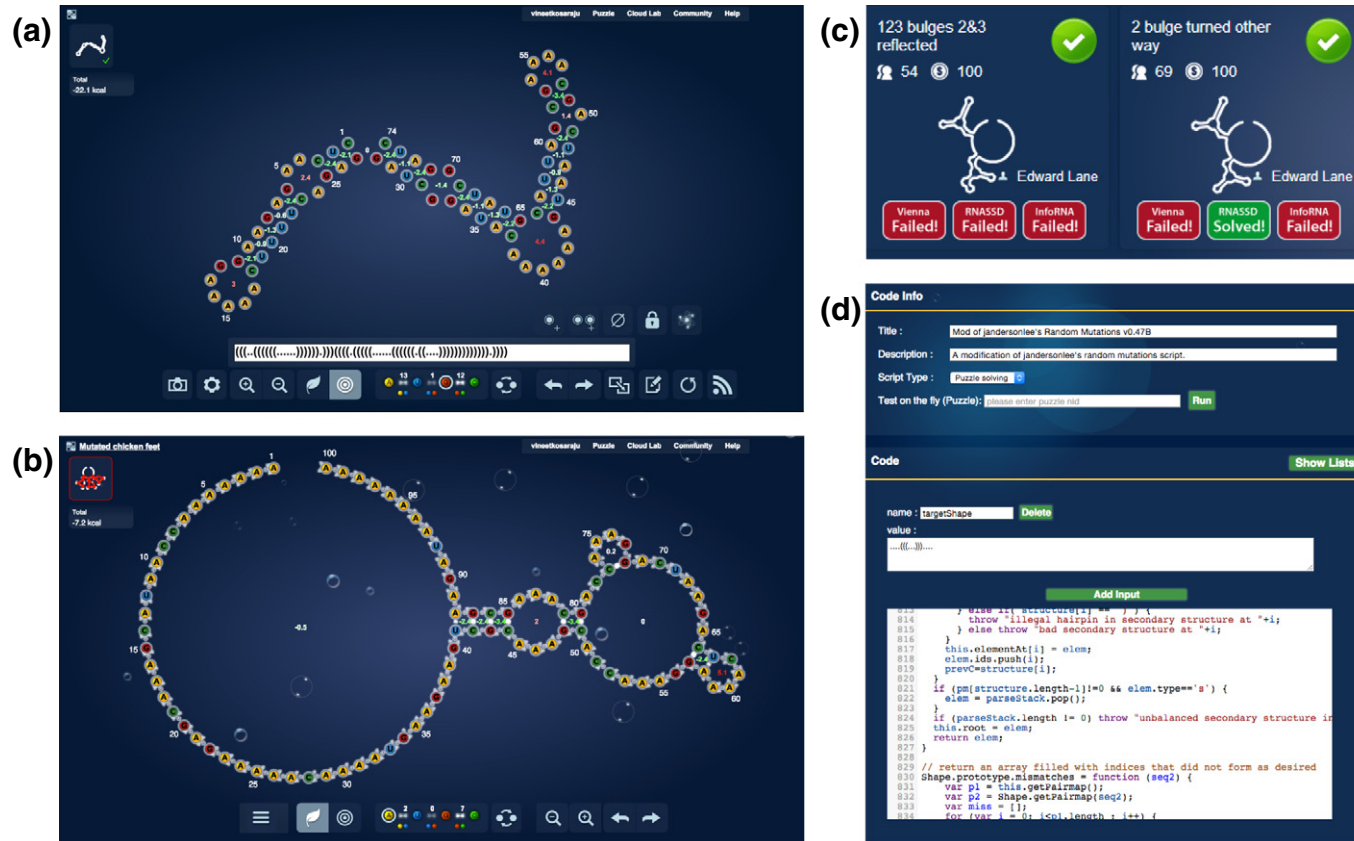
Fig. 1. Tools used by Eterna community to assess difficulty of RNA secondary structure design puzzles. (a) The puzzle maker interface allows players to define a secondary structure string or insert bases or base pairs at specified positions and then deploy these puzzles to other players to solve. (b) The puzzle solver interface enables players to select nucleotides and paint them over the structure, which can switch between natural and target modes. (c) After puzzle design, players are able to see which bots are able to solve their puzzles. (d) The EternaScript interface allows for players to create and test their own puzzle-solving algorithms.

that improved the distance from the desired secondary structure [2]. Other algorithms took similar approaches, introducing additional features such as hierarchical decomposition of the target structure (RNA-SSD) [6], probabilistic sampling of sequences (INFO-RNA) [7] and multiple scoring functions (DSS-Opt) [8]. NUPACK combined some of these features and introduced the ensemble defect, a scoring function based on base-pair probabilities [9], while MODENA introduced a genetic algorithm to optimize both structure stability and similarity to target [10]. Despite these advances, it remains difficult to distinguish, *a priori*, designable from intractable structures. Moreover, comparative benchmarks of design algorithms are not available, and it is unknown which structured features challenge which methods. Therefore, current design efforts can require multiple iterations to select a tractable secondary structure for a specific design problem with a specific design tool.

Assessing RNA designability is one of the main research areas of Eterna (previously "EteRNA"), a massive open laboratory that brings together tens of thousands of human participants ("players") to tackle RNA design problems[§] [11]. Here, we report insights from Eterna players who made use of a puzzle-solving interface, a puzzle creator tool, a puzzle selection interface and a solver scripting tool (Fig. 1) to create and analyze thousands of RNA secondary structures and their difficulty for sequence design. To help test which features are particularly challenging to design, Eterna integrated several automated solvers (RNAInverse, INFO-RNA and RNA-SSD) into the game (Fig. 1c), as well as an EternaScript framework enabling simple player-designed algorithms (Fig. 1d). These tools have allowed players to test numerous hypotheses about what makes puzzles difficult for these algorithms. While these studies have been described in many player-created documents (several compiled herein as Supporting Documents), they have not yet been presented in the formal scientific literature or subjected to tests outside the Eterna platform. Thus, here, we confirm these hypotheses on what makes RNA secondary structure design problems difficult using further independent tests, based on three independent inverse folding algorithms (NUPACK, DSS-Opt and MODENA) run on a separate supercomputer. Aside from these independent tests, most of the writing herein is drawn directly or closely adapted from writing in the original player-created documents.

We first describe several secondary structure features and specific structural idiosyncrasies that this internet-scale experiment has identified to be especially problematic for sequence design. Second, we describe the effects of symmetry on the design of RNAs, a less well-appreciated facet of difficult design challenges. Several of the discovered features arise frequently in natural RNA sequences and engineering challenges but, to our knowledge,

have not been previously noted as difficult for design. Finally, we introduce the Eterna100 benchmark, which we propose as a standard set of structures to be used for challenging and evaluating the next generation of automated RNA design algorithms.

Results

Secondary structure features

Based on manual creation and curation of thousands of puzzles through the Eterna puzzle designing and solving interface (Fig. 1), Eterna participants have identified several RNA secondary structure elements that result in the failure of state-of-the-art RNA design methods and player-designed algorithms. Most of these features can be simply rationalized: they introduce elements that have generally poor stability for any sequence and thus allow for the emergence of more stable alternative conformations. Beyond this simple rationalization, however, additional factors, such as the number of repetitions of each feature, also appear important in assessing design difficulty. To test these hypotheses, we evaluated six algorithms for their ability to solve various RNA design problems *in silico*. Henceforth, we define success as the design of a sequence whose minimum free-energy structure matches the target structure, as computed by the energy function used by the algorithm.

First, Eterna players postulated that short stems are major contributors to the difficulty of an RNA design puzzle. As illustrated by secondary structures in Fig. 2a, existing RNA design algorithms often fail to solve puzzles with many short stems and the difficulty increases as the number of stems increases. For example, *Shortie 4* and *Shortie 6* are essentially the same puzzle with different numbers of two base-pair stems. Algorithms such as NUPACK are able to solve the 2-stem *Shortie 4* but not its 4-stem sibling *Shortie 6* (colored squares in Fig. 2a). The difficulty of designing short stems has been previously suggested in computational studies [7] but does not seem to be widely known. For example, recent work on RNA origami tiles involves stems with only two base pairs that act as three-dimensional "dovetail" seams between parallel stacks of double helices [5] but may cause problems in larger origami constructions.

There is a further reason for the difficulty of short-stem puzzles besides the generally low stability of these features, which, to our knowledge, has not been previously noted. Since the sequence space for two base-pair stems is small, there are very few stable sequence combinations for these stems. If such stems occur once or a few times in a structure, they can be
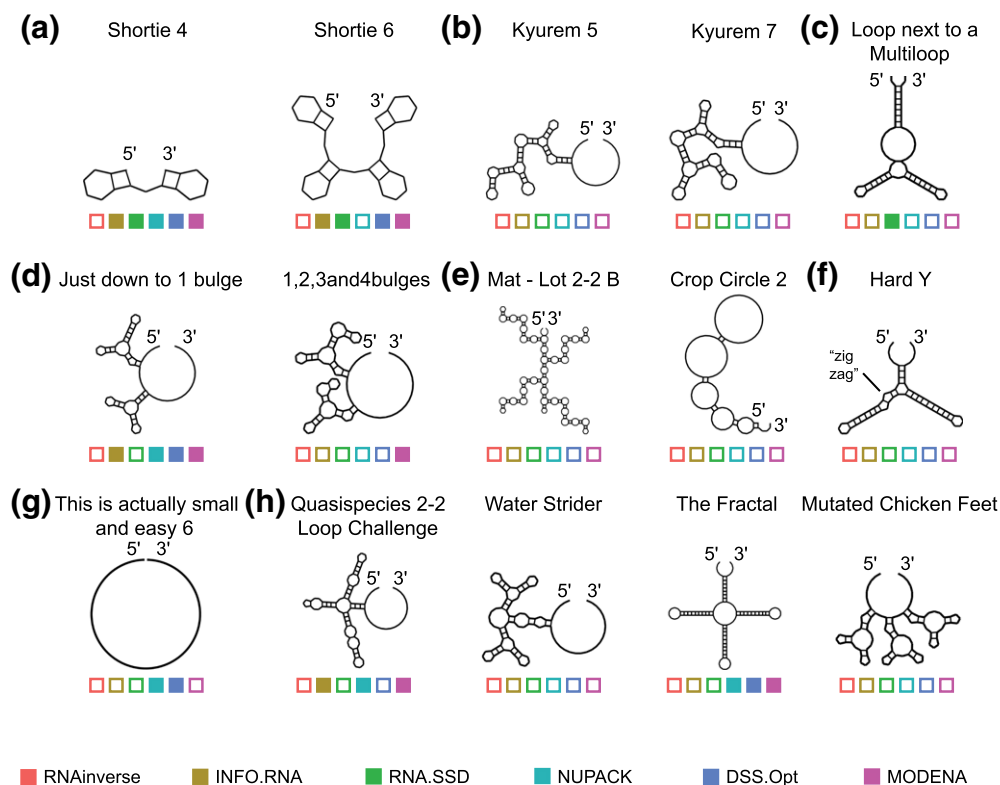
Fig. 2. RNA design puzzles from Eterna demonstrate features that make design difficult. Open or filled squares indicate failure or successful solutions, respectively, by existing RNA design algorithms—RNAInverse (red), INFO-RNA (yellow), RNA-SSD (green), NUPACK (cyan), DSS-Opt (blue) and MODENA (purple). (a) Stem length: *Shortie 4*, *Shortie 6*; (b) adjacent multiloops: *Kyurem 5*, *Kyurem 7*; (c) *Loop next to a Multiloop*; (d) bulges: just down to 1 bulge, 1, 2, 3 and 4 bulges; (e) internal loops: Mat—Lot 2-2 B, *Crop Circle 2*; (f) zigzags: *hard Y*; (g) simple puzzles: *This is ACTUALLY Small and Easy 6*; (h) quasi-species 2-2 loop challenge, *Water Strider*, *The Fractal*, *Mutated Chicken Feet*.

stabilized with one of the known stabilizing sequence combinations. However, when many of these stems are present in a target secondary structure, subsequences will necessarily have to be repeated in order to ensure that all stems are stable. This repetition of subsequences introduces opportunities for mispairing that must be "designed away" through careful positioning of subsequences into the structure. This issue is expected to increase the difficulty of design in large RNA structures that include series of nearby, repeated 2-bp stems (such as origami tiles in Ref. [5]) and may explain why natural RNAs, such as ribosomal RNAs, do not seem to take advantage of repeated sub-tiles or stems. Further examples of this principle of repetition will be described below.

The problem of short stems is worsened when the stems are flanked by multiloops (junctions) or bulges, as in the *Kyurem* puzzles (Fig. 2b). The design of multiloops often requires detailed optimization of the closing pairs of each stem, and when stems are difficult to maintain, this problem becomes exacerbated. There are extreme cases in which two loops are joined by a stem with only one base pair, such as in the puzzle *Loop next to a Multiloop*

(Fig. 2c); these are especially difficult, as the same base pair must close more than one loop. Even though these arrangements occur with some frequency in natural RNAs and are permitted in most *in silico* secondary structure prediction models, most RNA design algorithms have difficulty solving them. This is distinct from the idea of short stems because introducing a stronger base pair or permuting the stem pairs is often insufficient to stabilize the stem. These problems instead require the optimization of energies of neighboring loops and stems and are thus much more sensitive to the local sequence than other problems with short stems.

As an example, Fig. 3a illustrates a near-miss sequence solution created by a player-written puzzle-solving script for *Kyurem 7*, while Fig. 3b shows how a few changes to the design would have solved the puzzle. In Fig. 3a, the short stem between the bulge and multiloop (region outlined in red circles) is not predicted to form in the minimum free-energy solution. Strengthening the failing stem between the multiloop and bulge alone does not fix this near solution, but success is achieved by exchanging one closing pair on the multiloop from
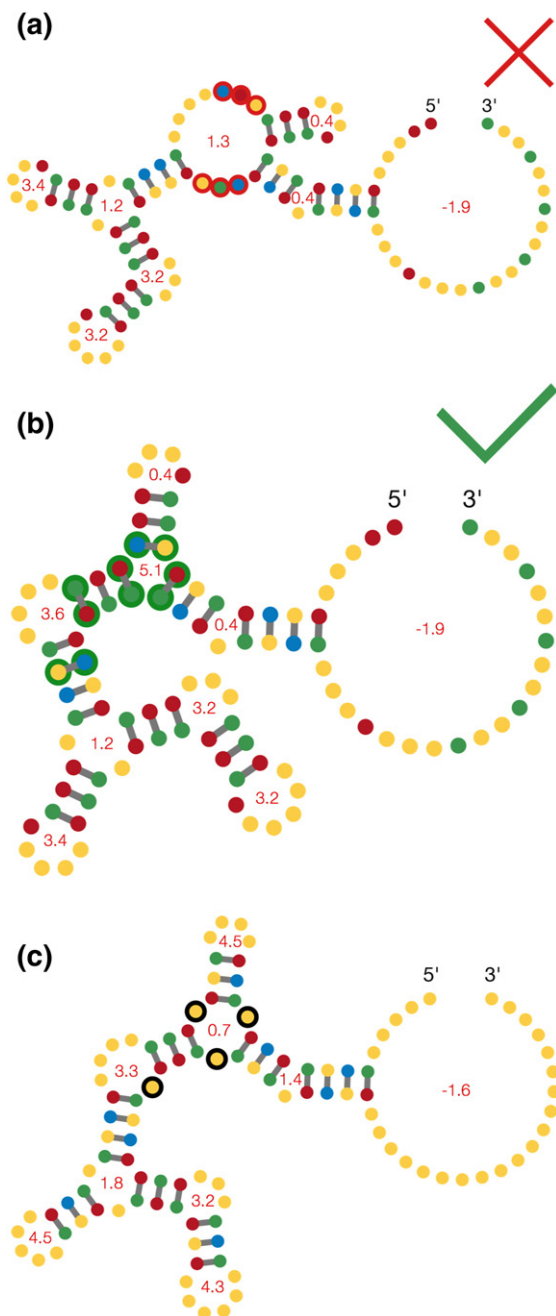
Fig. 3. A case study for RNA design—*Kyurem 7*. (a) A near-miss sequence design for *Kyurem 7* (see Fig. 2b) was designed by a player-created bot and misfolds only in one stem (red). (b) A successful solution with only a few base changes (green). (c) A slight variation in the *Kyurem 7* target secondary structure has only minor changes in the lengths of the multiloops but is much easier to solve due to the availability of low-energy designs for the expanded multiloops. Nucleotides are colored by base, with A in yellow, U in blue, G in red and C in green. Minimum free-energy structures and loop energies (kcal/mol) are based on the Turner 1999 parameters [1].

a GC to an AU, flipping another closing pair from a CG to a GC and flipping a third AU pair in an adjacent stem to strengthen it (Fig. 3b). These additional changes alter the energy of the potential misfolded states that occur relative to the target shape. These sorts of changes are routinely proposed by Eterna players to solve these puzzles but are not found by current automatic algorithms (Fig. 2b).

Bulges and internal loops within helices were also proposed to contribute to destabilization of RNA secondary structures and thereby to the general difficulty of designing sequences for these structures. Incremental introduction of additional bulges, as shown in Fig. 2d, resulted in failure by more of the design algorithms and fewer successful player solutions (Table S1). These interruptions within a stem disrupt the favorable stacking interactions between base pairs, increasing (worsening) the free energy of the target RNA conformation. Last, as shown in Fig. 2e, large internal loops, especially those bordered by short stems, present the problem of designing a low-energy loop to compensate for the short stems and overall high energy of the structure. All algorithms fail at these problems.

Overall, secondary structural elements that are typically higher in predicted free-energy change, such as multiloops with no unpaired bases, were generally viewed as being harder to design. For example, if the 0-0-0 multiloop (with 0 nucleotides separating the three stems) in *Kyurem 7* is replaced by a 1-1-1 multiloop (with single nucleotides separating the three stems) and the 4-0 bulge is replaced by a 4-1 asymmetric loop, these slightly lengthened loops allow for sequence solutions with more favorable energy (compare energies, Fig. 3b and c), and the overall structure becomes easier to solve.

The quantity and density of the previously described elements are important for determining puzzle difficulty. As a summary, players use a principle of least elements, which asserts that the fewer of the elements delineated in Fig. 2, the more likely a design is to be feasible. This principle allows the design difficulty of a target secondary structure to be gauged by eye. Further examples of this principle are provided in the benchmark described below.

Structural idiosyncrasies

Specific patterns of bulges were identified by Eterna players as particularly problematic regions for RNA design. The *hard Y* puzzle, shown in Fig. 2f, has relatively long stems but contains two consecutive bulges opposite each other, a motif that players named the "zigzag". The presence of this pattern close to a small multiloop, in an otherwise straightforward puzzle, causes most existing algorithms to fail. Zigzags appear uncommon in natural RNA structures, and we propose that their infrequency is related to the difficulty of designing them.

Players also noted that existing RNA design algorithms also fail on extremely simple problems of biological interest. *This is ACTUALLY Small and Easy 6*, shown in Fig. 2g, consists of 400 unpaired nucleotides. While setting the entire sequence to the same nucleotide is sufficient to force complete unpairing and solve the problem, these algorithms overcomplicate the design problem by randomly initializing the sequence, causing them to fold incorrectly. These types of overly simple designs are an unexpected class of difficult problems for current algorithms. Nevertheless, automating strategies for solving them will be important for designing RNA nanostructures that need to present long single-stranded stretches to other molecular machines for translation, splicing or reverse transcription.

Symmetry

Players observed that striking visual symmetry in a target secondary structure is typically a hallmark of a difficult problem for sequence design, as demonstrated by the failure of existing algorithms to solve puzzles with high symmetry (Fig. 2h).

The effect of symmetry on design puzzle difficulty appears mainly due to the presence of repeated elements. These elements may be similar or same-length stems, as described in the previous section. However, any other repeated structural motif can also lead to difficulty of symmetrical designs. The rationale is similar to the one described above for 2-bp stems: short, complex substructures, such as those in *Mutated Chicken Feet* (Fig. 2h), can only be solved by a highly constrained space of subsequences. Repetition of these substructures can result in highly similar sequences for each of the repeated elements, increasing the probability of mispairing and decreasing the probability of a successful fold, requiring careful optimization. Supporting
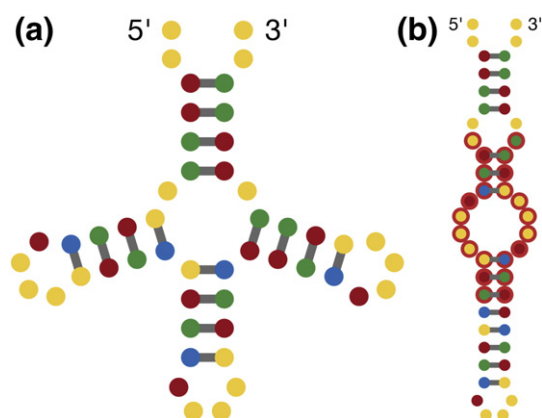
this "principle of repetition" as the underlying factor and not symmetry *per se*, the difficulty of these problems appears agnostic to the type of visually apparent symmetry: the symmetry can be axial (e.g., *Water Strider*) or translational (e.g., *Mutated Chicken Feet*), as depicted in Fig. 2h.

Additionally, although the repetition of secondary structure features increases the difficulty of computing a correctly folding sequence, when repeating substructures are combined with the factors described above, the difficulty can further decrease or increase. On one hand, *The Fractal* demonstrates symmetry with a stable hairpin element; long stems make this solvable by five of six algorithms (Fig. 2h). On the other hand, *Crop Circle 2* (Fig. 2e), which contains a repeated element with short stems and large loops, is intractable for all existing secondary structure design algorithms tested.

Finally, many puzzles that are visually symmetric also include a multiloop, which is typically a high-energy element, as discussed previously, and can conspire with repeating substructures, large loops or short stems to increase problem difficulty. In these multiloop-containing symmetric puzzles, a common misfold allows portions of symmetrically opposite structures to base pair and to replace a multiloop with a sequence of multiple simple stems and internal loops (Fig. 4).

In summary, visually apparent symmetry in a target secondary structure typically entails a number of features—repeated substructures, individually complex loops and multiloops at the axes or points of symmetry—that herald difficulty for sequence design. This observation may explain why large natural structured RNAs, such as ribosomes and self-splicing introns, have fractal-like secondary structures but are still not symmetric despite the ease of creating such repetitious structures through processes analogous to gene duplication [12]. For natural RNAs with near symmetry, such as riboswitches with two tandem aptamers that bind glycine, the sequences of cognate helices in the repeated aptamers are distinct, as might be expected. In addition, however, the lengths of the cognate helices are not identical [13], even though exact secondary structure symmetry would be expected to stabilize these RNAs' near-symmetric three-dimensional folds when bound to their small molecule targets [14,15]. The slight breaking of symmetry at the secondary structure level is a design rule that does not appear to be widely appreciated outside Eterna. Recognition of this rule may aid RNA nanoengineering efforts seeking to build large-scale tiles, polyhedra and tandem shRNAs and sgRNAs [3–5,16,17].

Fig. 4. An example of a common near-miss fold. A symmetric, multiloop-containing puzzle created by players, in which designs for the target structure (a) frequently mispair to create the same misfolded structure (b).

The Eterna100 benchmark

To test and help disseminate the principles described here, we have developed the Eterna100

(a)

(b)
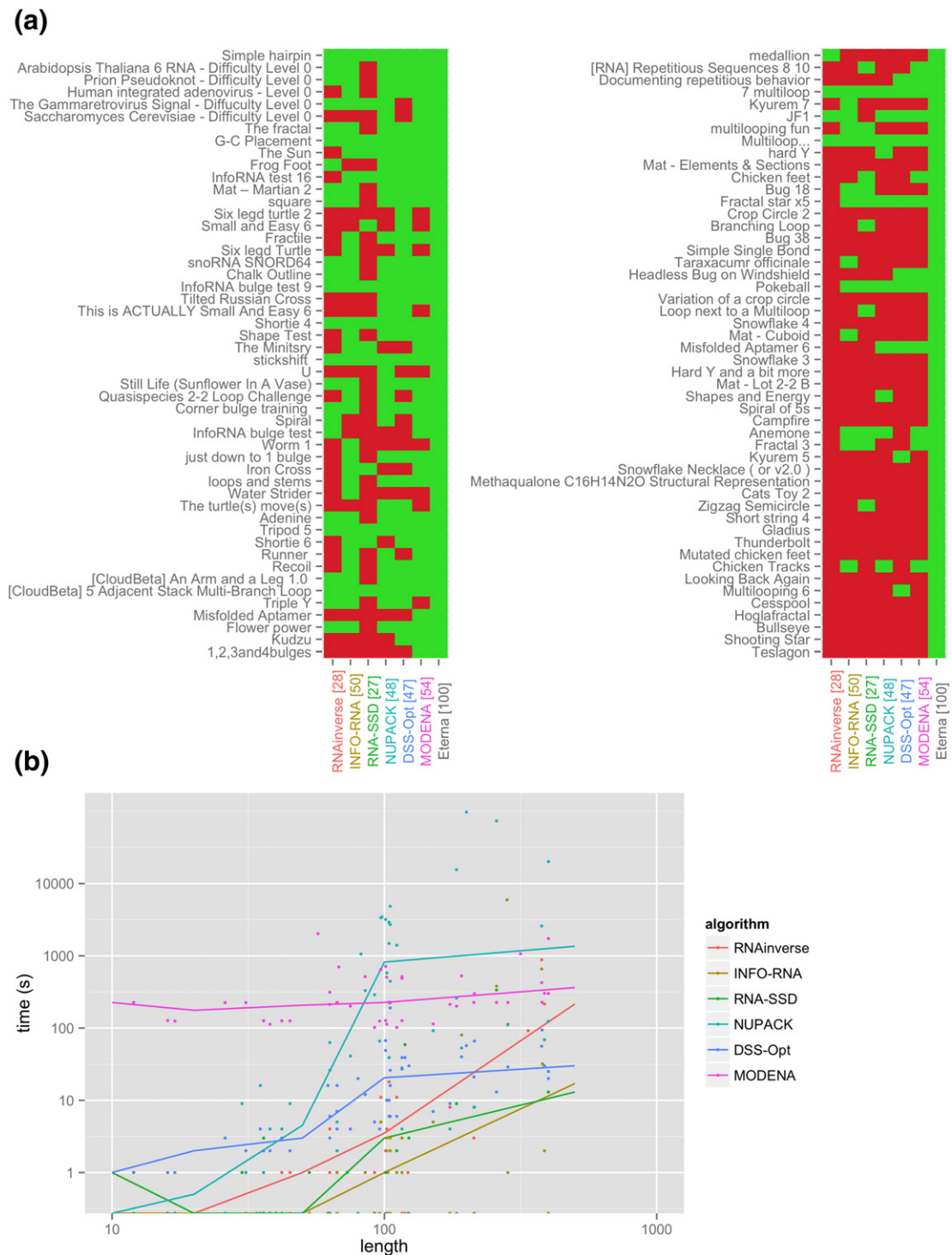
Fig. 5. Performance of existing algorithms on the Eterna100 benchmark. Six RNA design algorithms were evaluated using the Eterna100 benchmark. (a) The successes (green) and failures (red) are shown for each algorithm. The puzzles are ordered by the number of successful solvers on Eterna, from fewest to most, and the algorithms are labeled with the number of puzzles solved. (b) The amount of time required to reach a solution for puzzles of different lengths is shown for each algorithm. Lines show the median values over each bin of lengths.

benchmark for evaluating RNA design algorithms (Table S1). This set of 100 structures spans a wide range of lengths and difficulties, from short hairpins to complex 400-nucleotide designs. It includes all of the structures shown in Fig. 2, which exemplify the features we have found to make design difficult, as

well as additional structures that have different combinations of secondary structure features. The list also includes puzzles, like *Misfolded Aptamer* and *This is ACTUALLY Small and Easy 6*, whose difficulty for existing algorithms surprised us.

Figure 5 shows the performance of six current RNA design algorithms on these puzzles, highlighting the strengths and weaknesses of different methods. Five of the six algorithms seek sequences whose predicted minimum free-energy structure is the target structure, the same success conditions as are used in Eterna *in silico* challenges. The exception, NUPACK, optimizes the ensemble defect of the sequence, a partition function-based measure of the entire ensemble's deviation from the desired structure, and has not yet been optimized for long RNA lengths; we nevertheless included it due to its wide use. We chose not to include EteRNABot, as it was created to design for *in vitro* rather than *in silico* performance.

Top Eterna players were able to solve all 100 puzzles. Overall, MODENA is unable to handle structures of fewer than 10 bases but outperforms all other algorithms on some of the longest designs, solving 54 of the 100 puzzles. INFO-RNA solves a similar number of puzzles (50) but runs 100 times faster (gold vs. magenta, Fig. 5b). Despite these individual areas in which particular algorithms shine, most fare poorly on the harder puzzles. For example, symmetrical structures, including *Mutated Chicken Feet*, stump all of the algorithms but could be solved by players.

Discussion

Player-led scientific writing

This article has presented scientific insights collated from extensive write-ups by citizen scientist players with no training in biochemistry or bioengineering prior to their involvement in Eterna, including two of the lead authors. Despite the unusual origin of these insights and writing, both the citizen and conventional scientist authors are comfortable presenting the results, in wording identical with or closely adapted from the original player write-ups, due to independent rigorous tests involving new algorithms and supercomputer resources unavailable to the players during their studies. Internet-scale hypothesis generation and subsequent independent tests devised by expert groups has served as a working template for scientific discovery [11,18–20], but the expert groups have typically written the resulting publications. Our work illustrates that players can take the lead in manuscript writing, and we suggest that this updated template may relieve bottlenecks in disseminating scientific results from internet-scale projects and better reflect the intellectual ownership of reported discoveries.

Design lessons

Despite numerous algorithmic and experimental testing advances addressing the inverse RNA folding problem, a simple set of guidelines for which RNA secondary structures are more or less amenable to design has not been available. Citizen scientist participants of Eterna have now delineated specific structural features that increase the difficulty of the inverse RNA folding problem. These insights include relating average stem length with problem difficulty, a principle of least elements to reduce complexity, an avoidance of specific structural motifs such as the zigzag and the avoidance of repetitive elements and symmetrical structures. We have confirmed these insights herein through independent tests with six widely used RNA design algorithms. We have also noted how biological RNA molecules appear to avoid difficult features such as exact symmetry. Recent RNA engineering efforts that seek to express RNAs in tandem arrays, to present unpaired RNA stretches available for recognition or to create complex nanostructures may have trouble scaling up secondary structure designs that violate these principles.

Current state-of-the-art RNA design algorithms currently do not evaluate *a priori* the difficulty of designing a specific RNA secondary structure. This makes it difficult for algorithms to adapt and automatically adjust to puzzle features or to gracefully quit when a puzzle is overly difficult or impossible to solve *in silico*. Future algorithms might by improved by explicitly recognizing these features in RNA secondary structure design problems and applying strategies specific to each feature. For instance, one common Eterna player strategy is to modify the strength of RNA stacks by adjusting the amount of G-C or A-U base pairs based on the average stem length. In addition, "boosts", or sequences that allow for more energetically favorable loops, can be used to stabilize local secondary structure. A more detailed player strategy involves using a compiled knowledge of which sequences solve specific substructures, such as zigzags, long stretches of unpaired residues or single-pair stems between long loops, and placing them first. Algorithms challenged with symmetric/repetitive problems could request more computational time for those cases. Given the success of Eterna players on even the hardest problems (Fig. 5), we are optimistic that integrating their strategies into algorithms will lead to improvement in automated RNA secondary structure design.

Toward experiments

For the purposes of this paper, we focus on obtaining *in silico* solutions, or sequences that fold into the intended structure according to

computational folding models. *In vitro* and *in vivo* tests [11] introduce additional factors that complicate the problem further. Distinct from this study, which assumes a specific energy model of RNA folding, *in vitro* design requires additional knowledge of which structure and sequence features are more likely to be sensitive to inaccuracies in current energy models of RNA folding. An example is the repetition of long subsequences in a design—even if a design is predicted by a given energy model to fold into a stable structure with a low probability of misfolding, such sequence repetition risks misfolding that might be exposed in *in vitro* tests [11,21].

The Eterna laboratory has already generated an abundance of chemical mapping data characterizing player designs, and the rapid improvement of player designs across multiple rounds of synthesis is evidence that players have developed a predictive intuition for how to design RNA molecules that will fold correctly. These experiments and analysis have already allowed for the identification of specific features that correlate with the success of player designs in the laboratory [11], strategies to surmount these challenges and proposal of rules that expand the *in silico* principles for design difficulty, described herein, to the problem of predicting design difficulty for *in vitro* tests. Prospective wet-laboratory tests of these insights, expanding the *in silico* tests presented here, are possible with Eterna's current massively parallel experimental pipeline [22], which tests 10,000 designs per monthly round and will provide the most useful framework for future RNA engineering efforts. Finally, multistate riboswitch design puzzle creation and solving tools (see also Refs. [23–25]) are now available in Eterna, along with large-scale experimental tests. A similar study to the present one detailing features that increase the difficulty of riboswitches and providing a benchmark for switch puzzles is an important next investigation.

Materials and Methods

For players' in-game tests, RNAInverse 1.8, INFO-RNA 2.0 and RNA-SSD were run on all Eterna puzzles on an Amazon EC2 instance. All puzzles were attempted five times by each algorithm with a total time limit of 2 h. Eterna players conducted experiments using a puzzle maker interface and the automatic execution of these three design algorithms to determine the weaknesses of these design algorithms. Players also used the EternaScript framework to design their own JavaScript-based puzzle solvers. One group of players used iterative development (the "Random Mutation" series of scripts) to develop a heuristic solver algorithm (see Supporting Documents). After each development cycle, the script was run against a benchmark set of puzzles and weaknesses were identified based on failures, allowing for further adaptations of the algorithm. Many of these original benchmark puzzles are part of the Eterna100, and the resulting insights were collated by players into Google documents (see Supporting Documents) and wiki pages available through the Eterna wiki[ll].

For the validation tests herein on the proposed Eterna100 benchmark, RNAInverse 2.1.9, INFO-RNA 2.1.2, NUPACK 3.0.5, RNA-SSD, DSS-Opt and MODENA were selected as a representative set of existing RNA design algorithms. Each secondary structure was run through all six algorithms using default parameters, with five attempts and a time limit of 24 h for each attempt. The computation was carried out on Intel Xeon Processors E5-2650. NUPACK uses its own custom fold function, based on the Turner 2004 parameter set [26], while the other five algorithms use the RNAfold function from ViennaRNA 2.1.9, based on the Turner 1999 parameters [27]. Eterna uses the fold function from ViennaRNA 1.8.5, which is also based on the Turner 1999 parameters. We chose to allow these differences in energetic parameters in order to produce an evaluation of each algorithm by its own favored rule set. Each solution was evaluated using the folding function used by the design algorithm to confirm whether or not the minimum free-energy structure corresponded to the input structure.

Appendix A. Supplementary data

Supplementary data to this article can be found online at http://dx.doi.org/10.1016/j.jmb.2015.11.013.

‡A complete list of the Eterna players can be found in Dataset S1.
§http://eternagame.org/.
‖http://eternawiki.org/wiki/.

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